

# Vector Network Analyzers Fundamentals

*Axel Hahn & Ansgar Lessmann*

*12/05/2022*

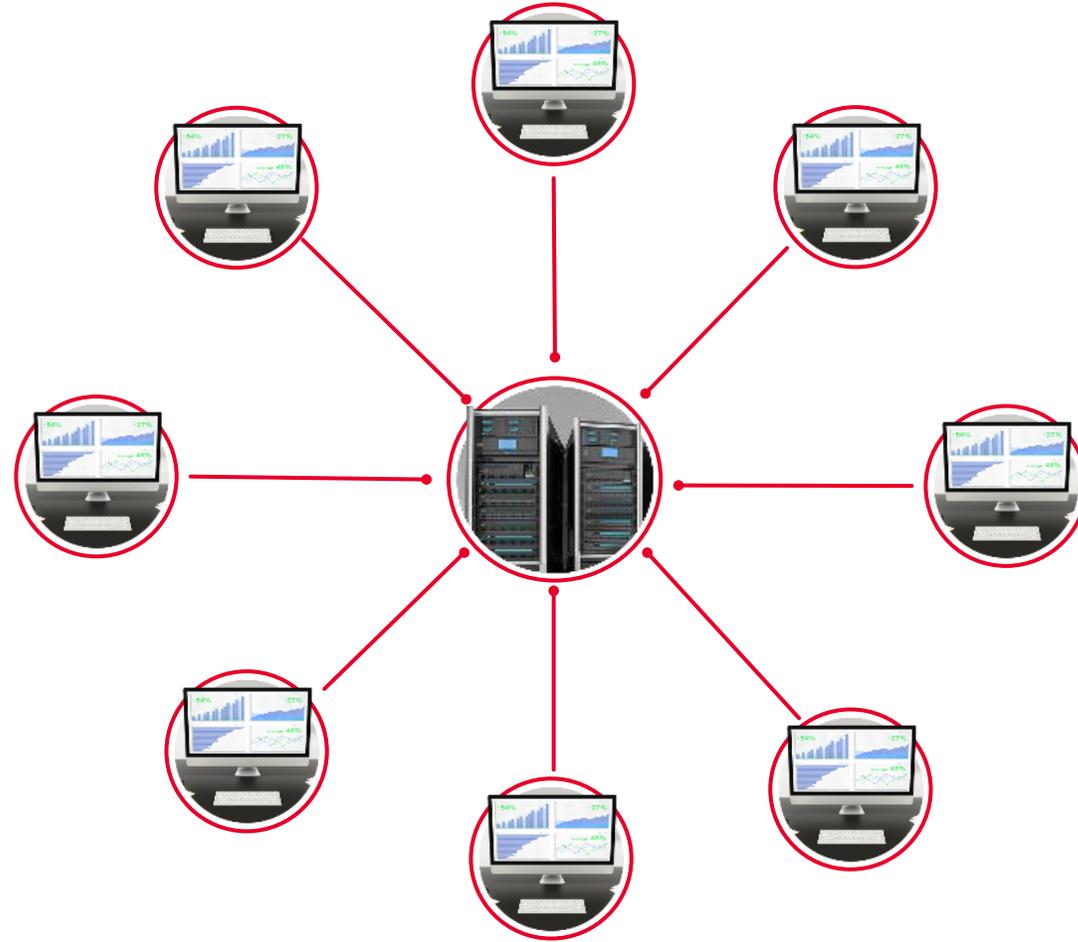
*Solutions Engineering – Keysight Technologies*



# Agenda

- What is a Network Analyzer?
- Transmission Lines and S-Parameters
- Network Analyzer Block Diagram
- Network Analysis Measurements
- Calibration and Error Correction

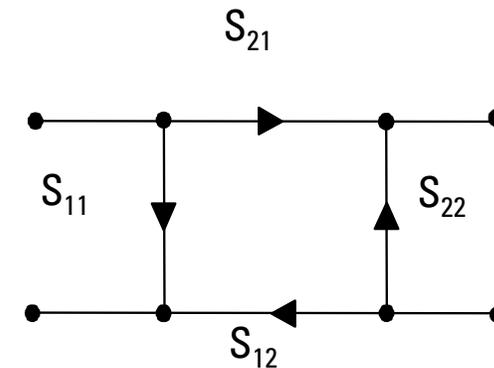
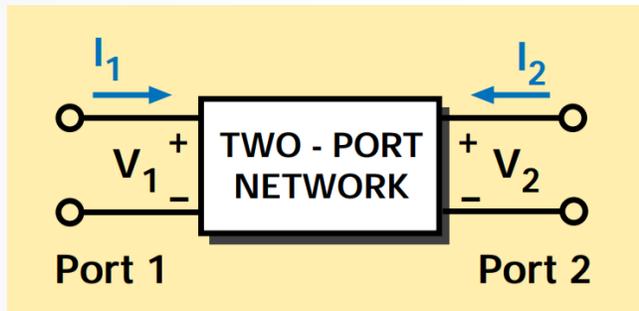
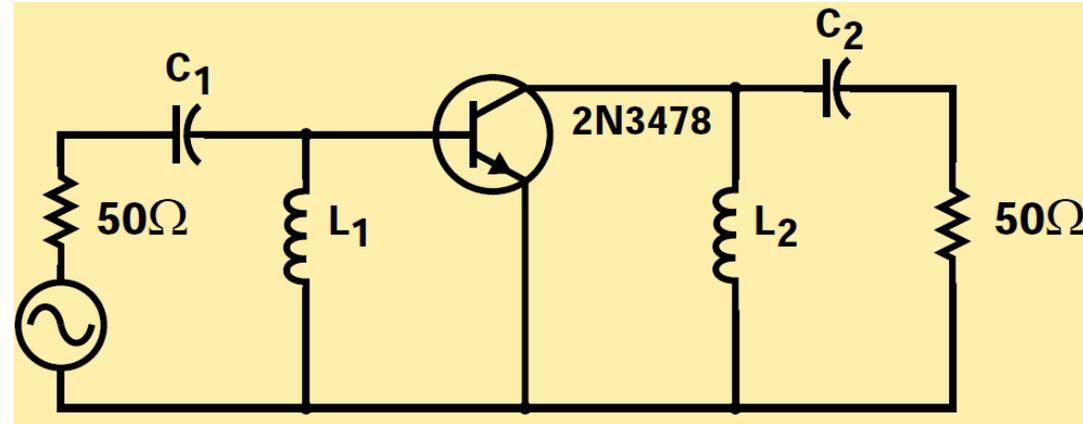
# Network Analysis is NOT the analysis of...



Computers, Network/protocol performance etc...

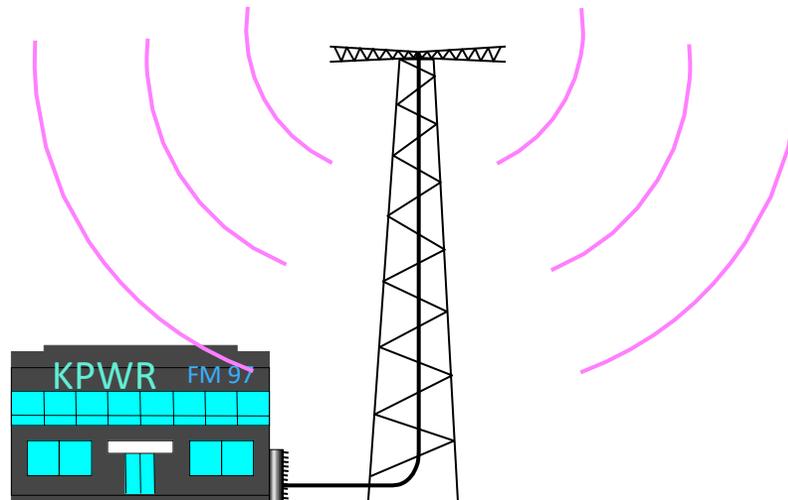
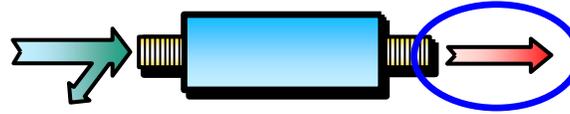
# What is a Network Analyzer?

A network analyzer is an instrument that measures the network parameters of electrical networks.



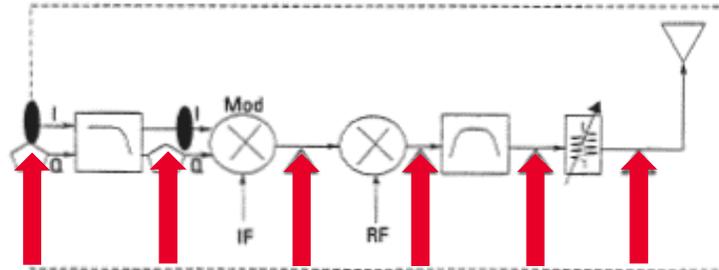
# Why Do We Need to Test Components?

- Verify specifications of “building blocks” for more complex RF systems
- Ensure distortionless transmission of communications signals
  - Linear: constant amplitude, linear phase / constant group delay
  - Nonlinear: harmonics, intermodulation, compression, X-parameters
- Ensure good match when absorbing power (e.g., an antenna)

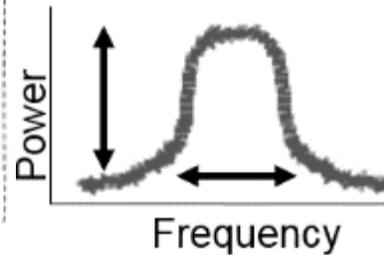


# Transmit Receive Design Challenges

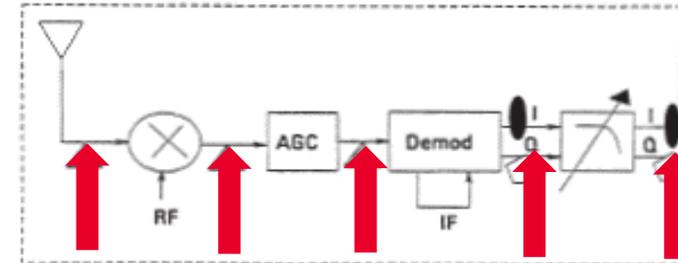
## TRANSMIT



- Output Power
- Operating Frequency
- Environment/Interference
- Noise



## RECEIVE

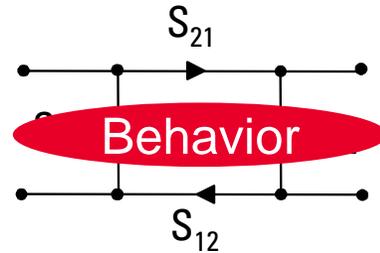


- Sensitivity
- Adjacent Channel Selectivity
- Operating Frequency
- Environment/Interference
- Noise
- Dynamic Range

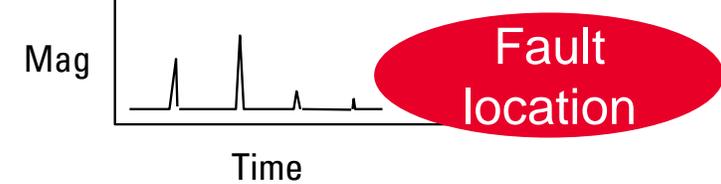
End goal: maximize link budget, fidelity & efficiency

# The Need for Both Magnitude and Phase

1. Complete characterization of linear networks



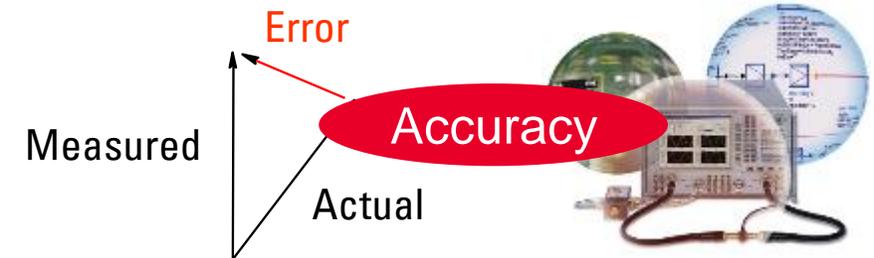
4. Time-domain characterization



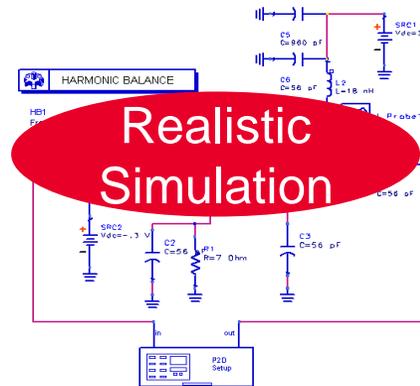
2. Complex impedance needed to design matching circuits



5. Vector-error correction



3. Complex values needed for device modeling



6. X-parameter (nonlinear) characterization

Pre-distortion

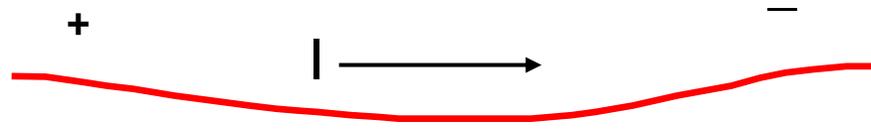
# Agenda

- What is a Network Analyzer?
- **Transmission Lines and S-Parameters**
- Network Analyzer Block Diagram
- Network Analysis Measurements
- Calibration and Error Correction

# Transmission Line Basics

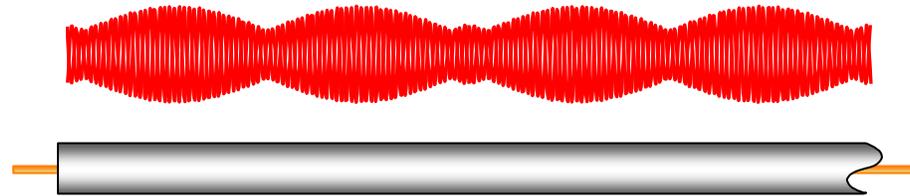
- Low Frequencies

- Wavelengths  $\gg$  wire length
- Current (I) travels down wires easily for efficient power transmission
- Measured voltage and current not dependent on position along wire



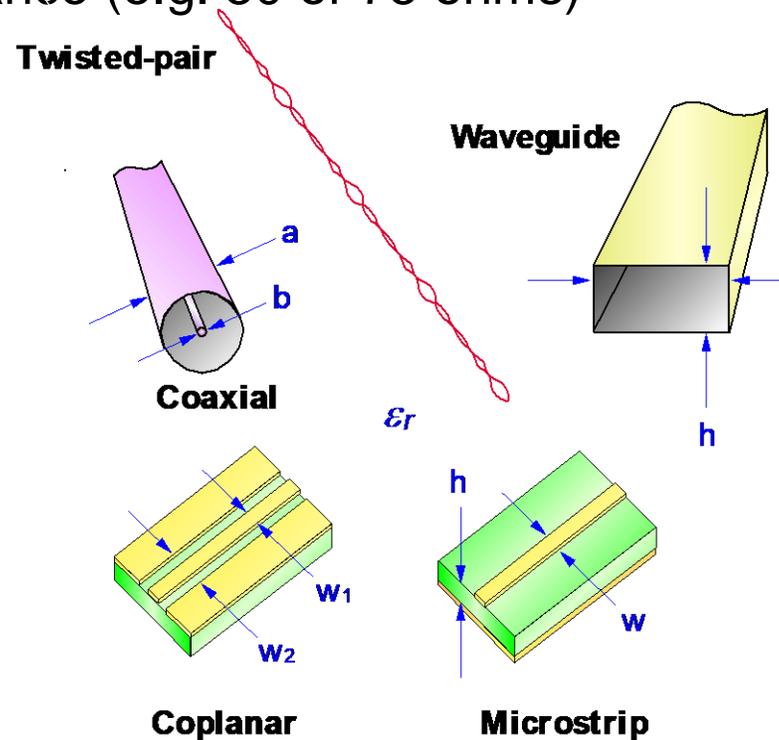
- High Frequencies

- Wavelength  $\sim$  or  $\ll$  length of transmission medium
- Need transmission lines for efficient power transmission
- Matching to characteristic impedance ( $Z_0$ ) is very important for low reflection and maximum power transfer
- Measured envelope voltage dependent on position along line



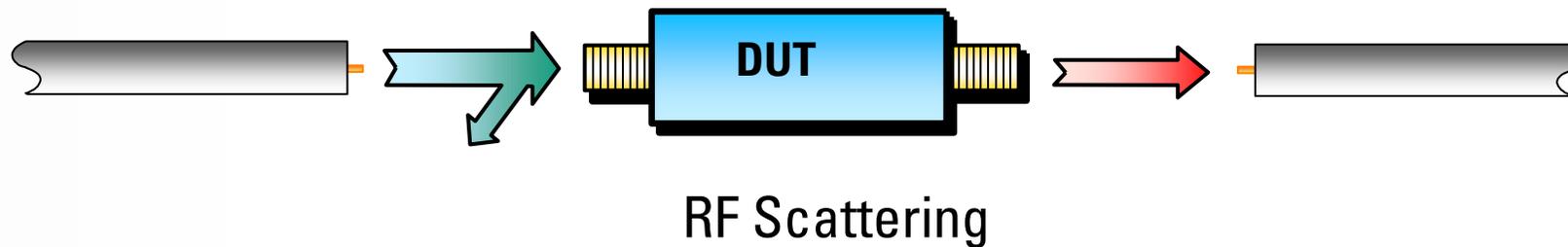
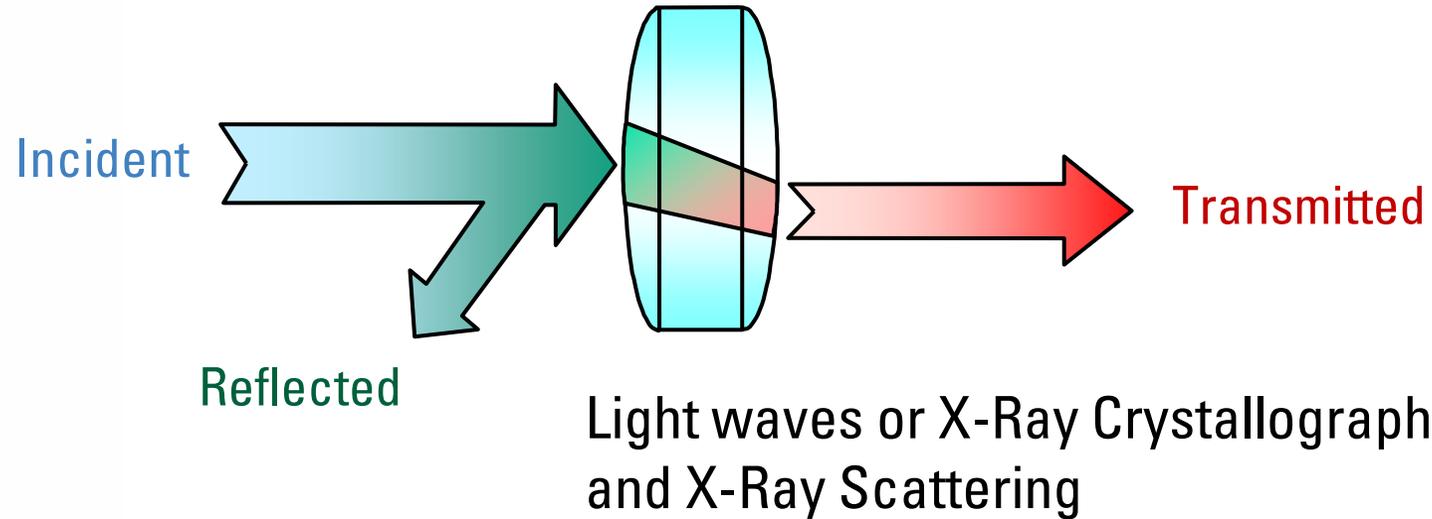
# Transmission line $Z_0$

- $Z_0$  determines relationship between voltage and current waves
- $Z_0$  is a function of physical dimensions and  $\epsilon_r$
- $Z_0$  is usually a real impedance (e.g. 50 or 75 ohms)

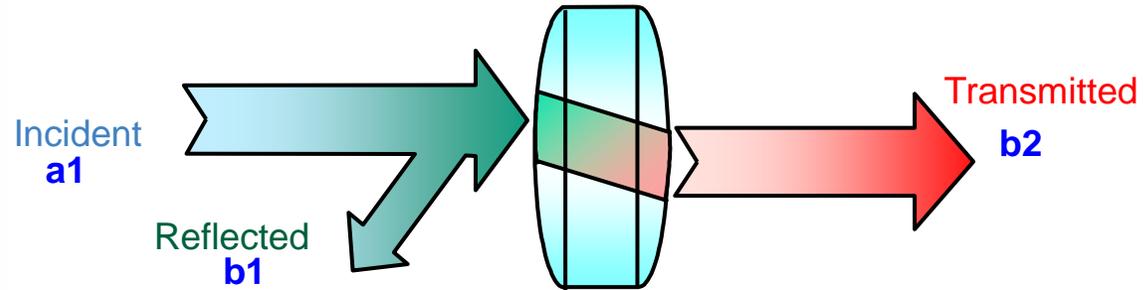


For more information on transmission line basics:  
<http://literature.cdn.keysight.com/litweb/pdf/5965-7917E.pdf>

# RF Energy Transmission

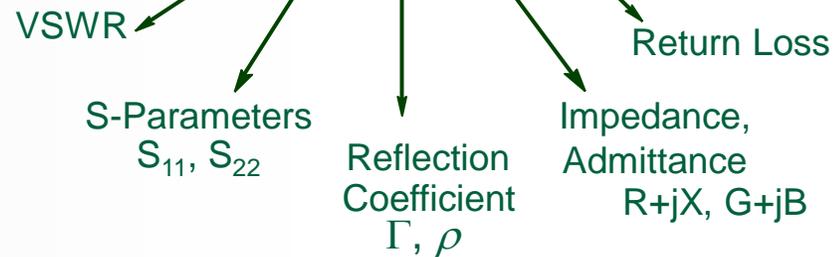


# High-frequency Device Characterization



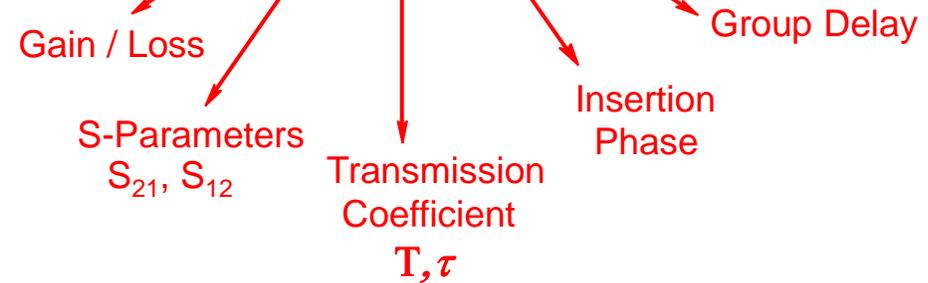
## REFLECTION

$$\frac{\text{Reflected}}{\text{Incident}} = \frac{b1}{a1}$$



## TRANSMISSION

$$\frac{\text{Transmitted}}{\text{Incident}} = \frac{b2}{a1}$$



# Reflection Parameters

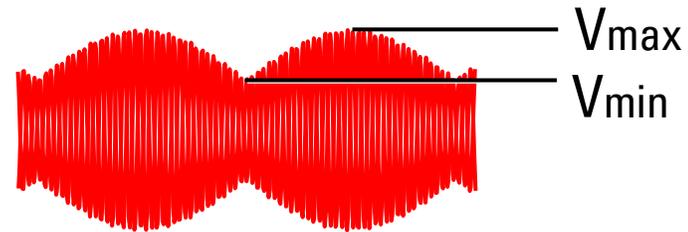
$$\text{Reflection Coefficient} = \Gamma = \frac{V_{\text{reflected}}}{V_{\text{incident}}} = \rho \angle \Phi = \frac{Z_L - Z_0}{Z_L + Z_0}$$

$$\rho = |\Gamma|$$

$$\text{Return loss} = -20 \log(\rho)$$

$$\text{Colloquially: Return loss} = 20 \log(\rho)$$

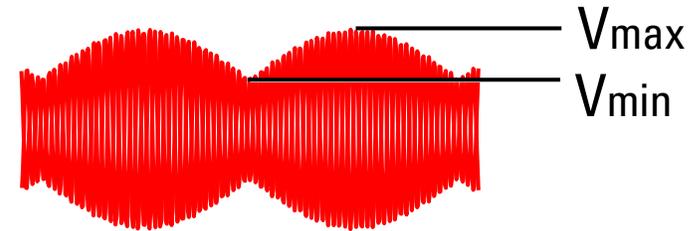
$$\text{Voltage Standing Wave Ratio} = \frac{1 + \rho}{1 - \rho}$$



# Reflection Parameters

Reflection Coefficient =  $\Gamma = \frac{V_{\text{reflected}}}{V_{\text{incident}}} = \rho \angle \Phi = \frac{Z_L - Z_o}{Z_L + Z_o}$

Voltage Standing Wave Ratio =  $\frac{1 + \rho}{1 - \rho}$



	<b>No reflection</b> ( $Z_L = Z_o$ )		<b>Full reflection</b> ( $Z_L = \text{open, short}$ )
0		1	
$(-\infty)$ dB		0 dB	
1		$\infty$	

For more information on reflection/transmission parameter basics:  
<http://literature.cdn.keysight.com/litweb/pdf/5965-7917E.pdf>

# Characterizing Unknown Devices

## USING PARAMETERS (H, Y, Z, S) TO CHARACTERIZE DEVICES

- Gives linear behavioral model of our device
- Measure parameters (e.g. voltage and current) versus frequency under various source and load conditions (e.g. short and open circuits)
- Compute device parameters from measured data
- Predict circuit performance under any source and load conditions

### *H-parameters*

$$V_1 = h_{11}I_1 + h_{12}V_2$$

$$I_2 = h_{21}I_1 + h_{22}V_2$$

(Hybrid)

### *Y-parameters*

$$I_1 = y_{11}V_1 + y_{12}V_2$$

$$I_2 = y_{21}V_1 + y_{22}V_2$$

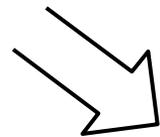
(Admittance)

### *Z-parameters*

$$V_1 = z_{11}I_1 + z_{12}I_2$$

$$V_2 = z_{21}I_1 + z_{22}I_2$$

(Impedance)

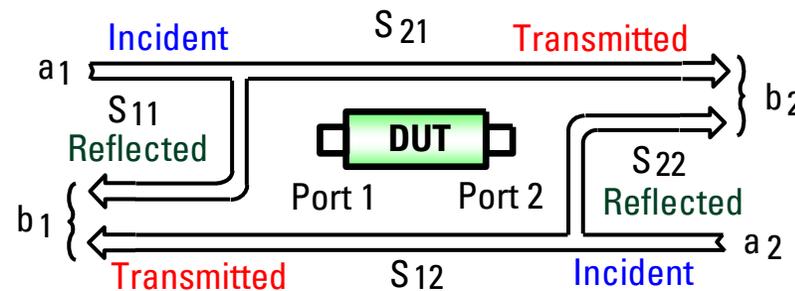


$$h_{11} = \left. \frac{V_1}{I_1} \right|_{V_2=0} \quad (\text{requires } \mathbf{short\ circuit})$$

$$h_{12} = \left. \frac{V_1}{V_2} \right|_{I_1=0} \quad (\text{requires } \mathbf{open\ circuit})$$

# Why Use Scattering, S-Parameters?

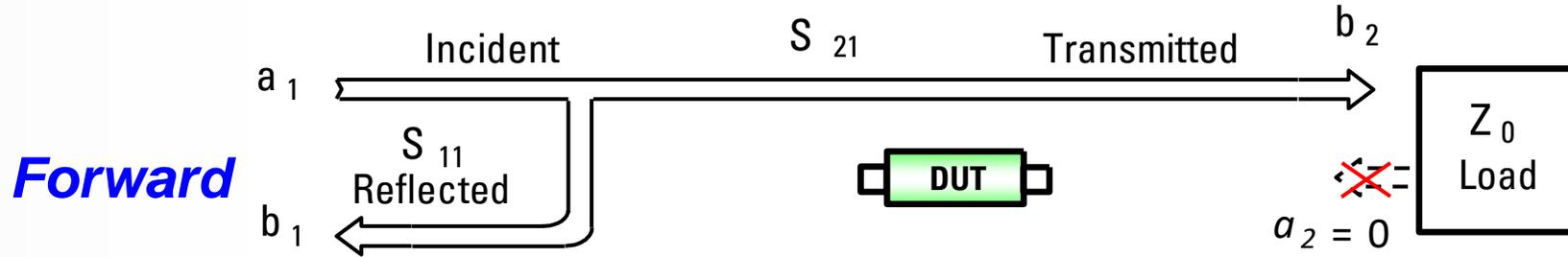
- Relatively easy to **obtain** at high frequencies
  - Measure voltage traveling waves with a vector network analyzer
  - Don't need shorts/opens (can cause active devices to oscillate or self-destruct)
- Relate to **familiar** measurements (gain, loss, reflection coefficient ...)
- Can **cascade** S-parameters of multiple devices to predict system performance
- Can **compute** H-, Y-, or Z-parameters from S-parameters if desired
- Can easily import and use S-parameter files in **electronic-simulation** tools



$$b_1 = S_{11} a_1 + S_{12} a_2$$

$$b_2 = S_{21} a_1 + S_{22} a_2$$

# Measuring S-Parameters

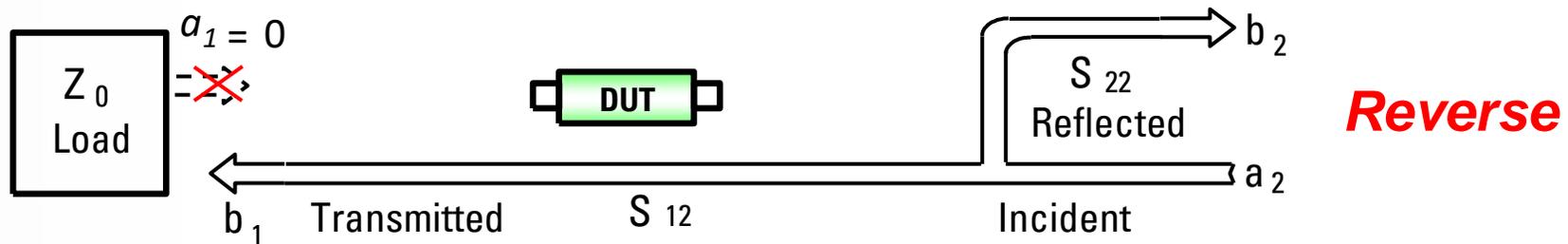


$$S_{11} = \frac{\text{Reflected}}{\text{Incident}} = \frac{b_1}{a_1} \Big|_{a_2 = 0}$$

$$S_{21} = \frac{\text{Transmitted}}{\text{Incident}} = \frac{b_2}{a_1} \Big|_{a_2 = 0}$$

$$S_{22} = \frac{\text{Reflected}}{\text{Incident}} = \frac{b_2}{a_2} \Big|_{a_1 = 0}$$

$$S_{12} = \frac{\text{Transmitted}}{\text{Incident}} = \frac{b_1}{a_2} \Big|_{a_1 = 0}$$



# Equating S-Parameters With Common Measurement Terms



$S_{11}$  = forward reflection coefficient (*input match*)

$S_{22}$  = reverse reflection coefficient (*output match*)

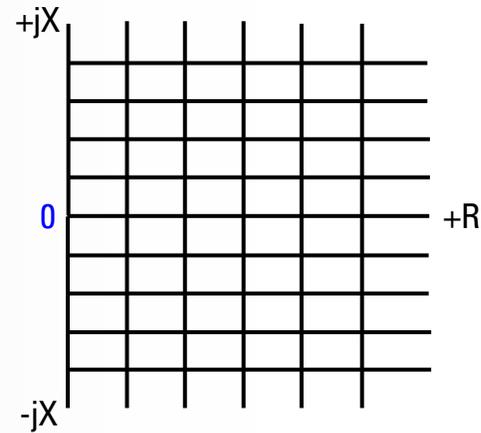
$S_{21}$  = forward transmission coefficient (*gain or loss*)

$S_{12}$  = reverse transmission coefficient (*isolation*)

**Remember S-parameters are inherently complex, linear quantities – however, we often express them in a log-magnitude format**

# Smith Chart Review

QUICKLY AND EASILY GET IMPEDANCE

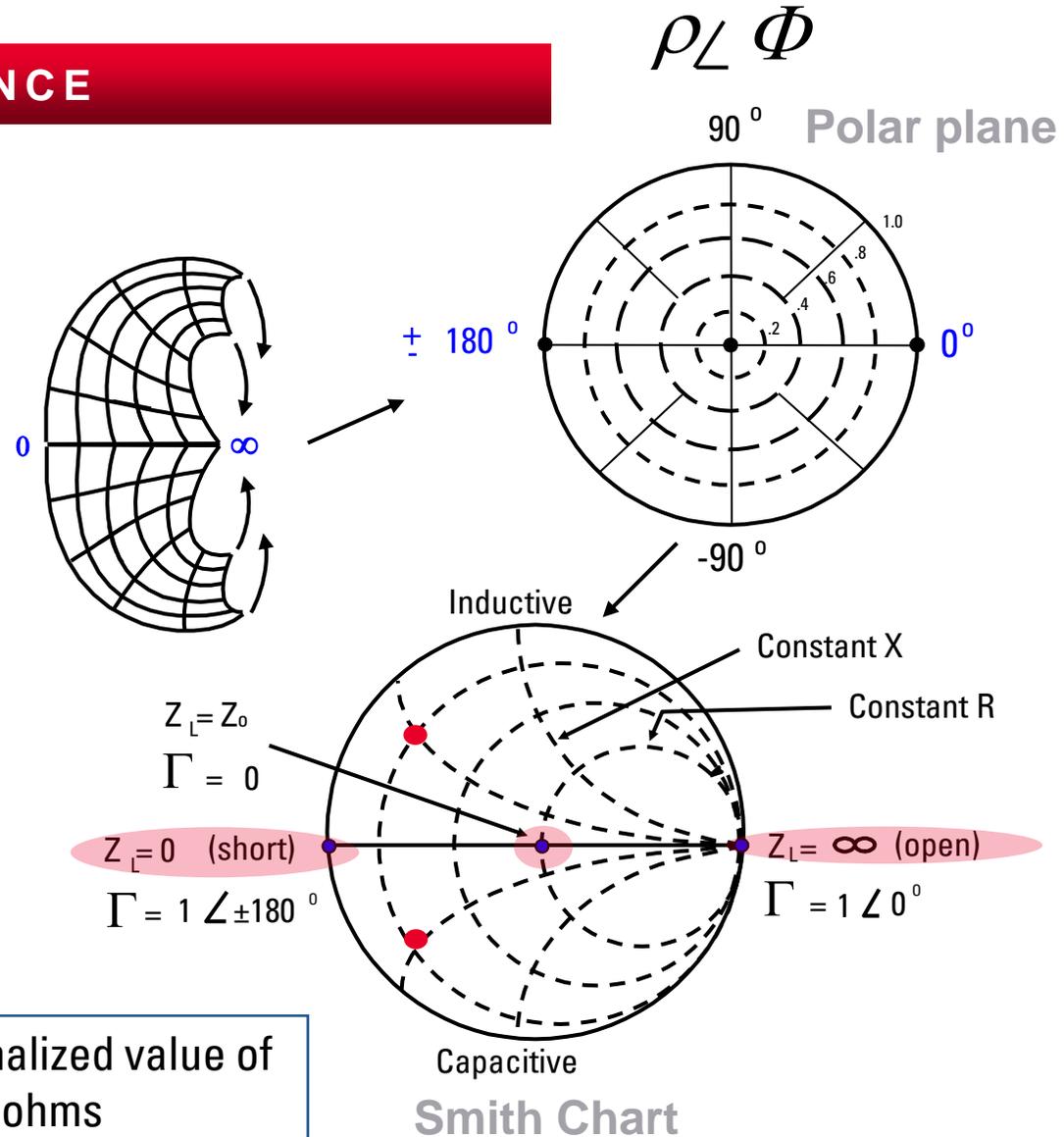


Rectilinear impedance plane

i.e:  $R+jX$ ,

Smith Chart maps rectilinear impedance plane onto polar plane

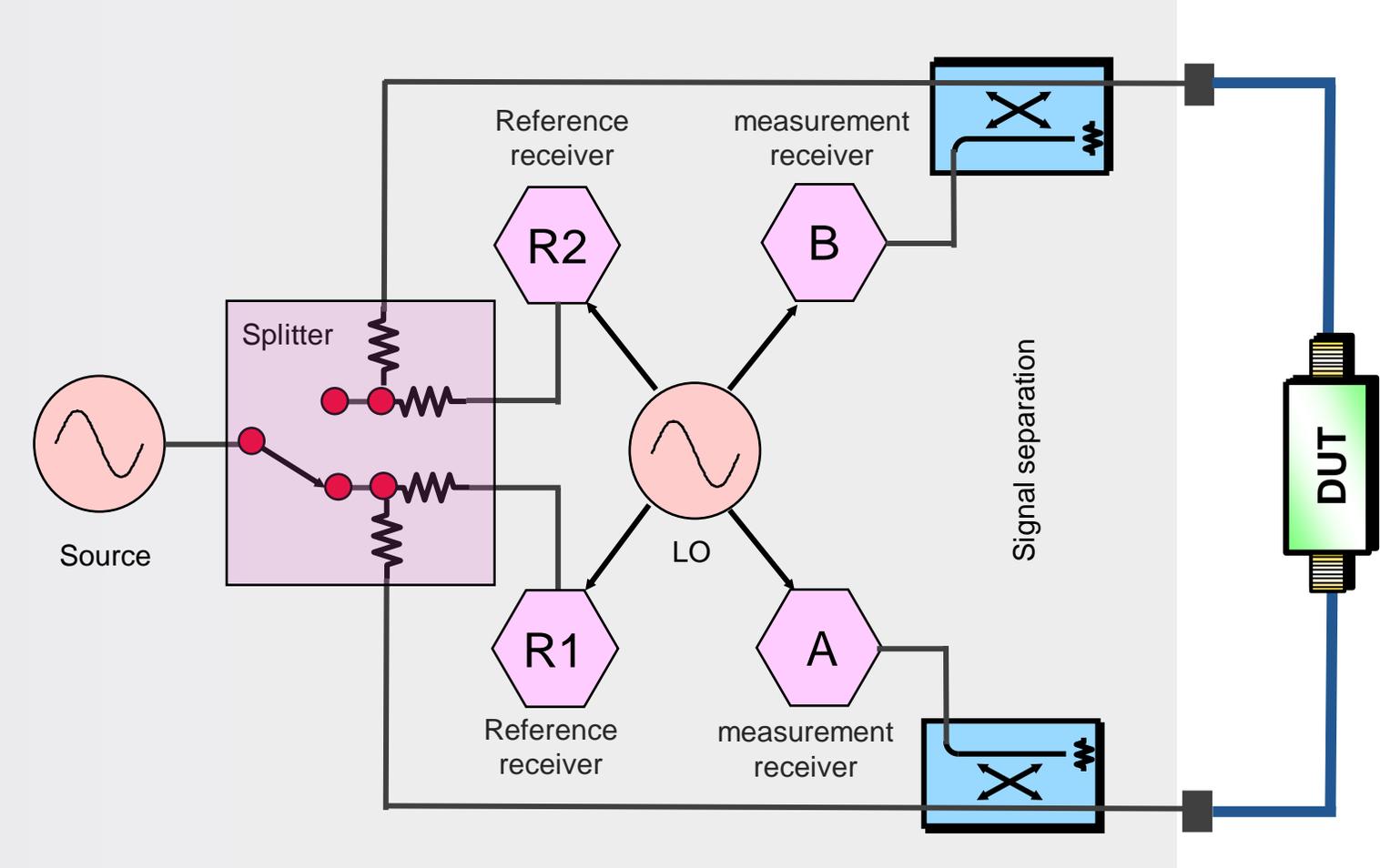
Example: in a 50-ohm system, a normalized value of  $0.3 - j0.15$  becomes  $15 - j7.5$  ohms



# Agenda

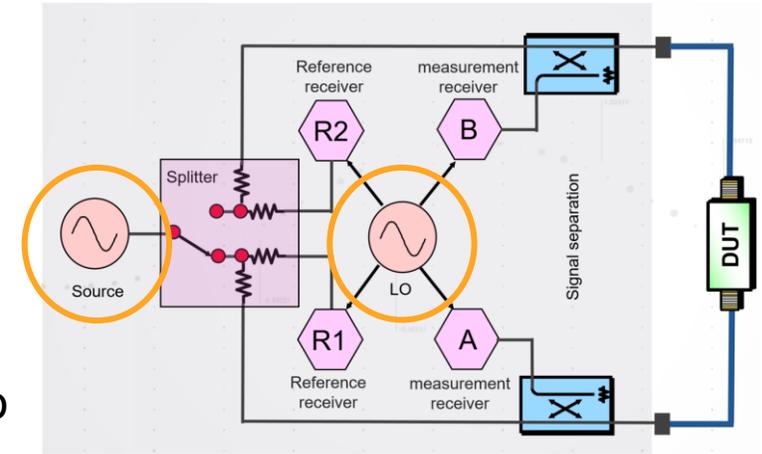
- What is a Network Analyzer?
- Transmission Lines and S-Parameters
- **Network Analyzer Block Diagram**
- Network Analysis Measurements
- Calibration and Error Correction

# Generalized Network Analyzer Block Diagram



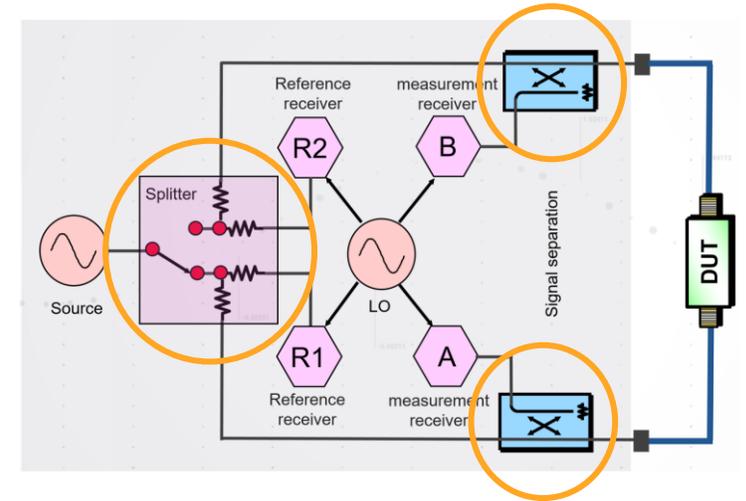
# Source

- Supplies stimulus for system
- Can sweep frequency or power
- Traditionally NAs had one signal source
- Modern NAs have the option for a second internal source and/or the ability to control external source
  - Can control an external source as a local oscillator (LO) signal for mixers and converters
  - Useful for mixer measurements like conversion loss, group delay

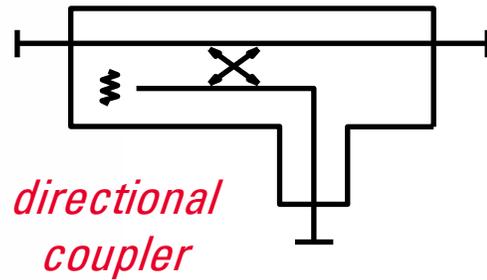
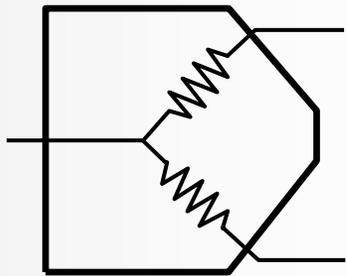


# Signal Separation

- Measure incident signal for reference
- Separate incident and reflected signals

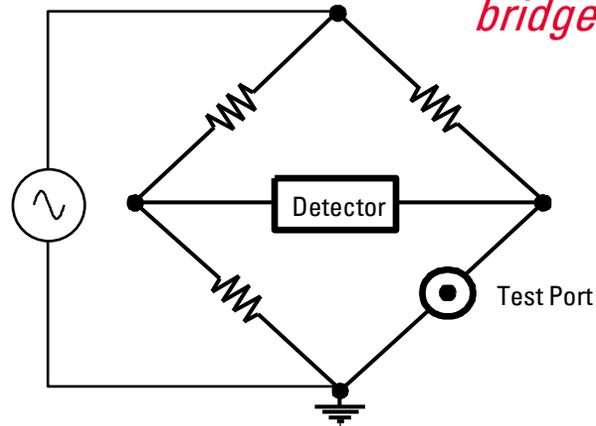


*splitter*



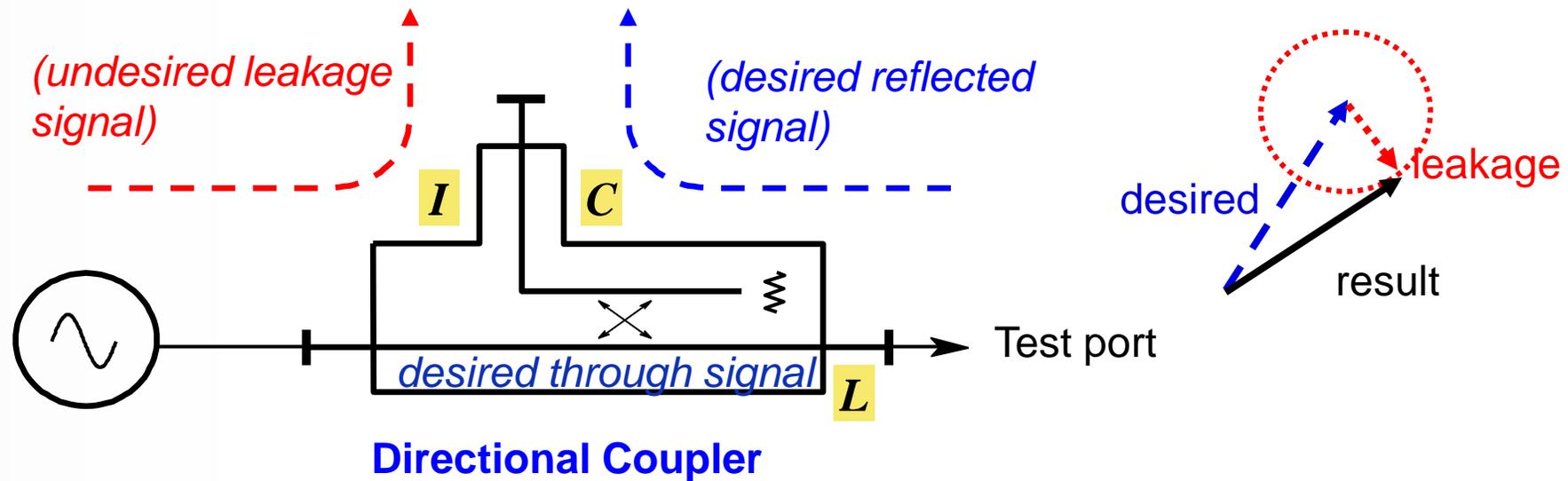
*directional coupler*

*bridge*



# Directional Coupler & Directivity

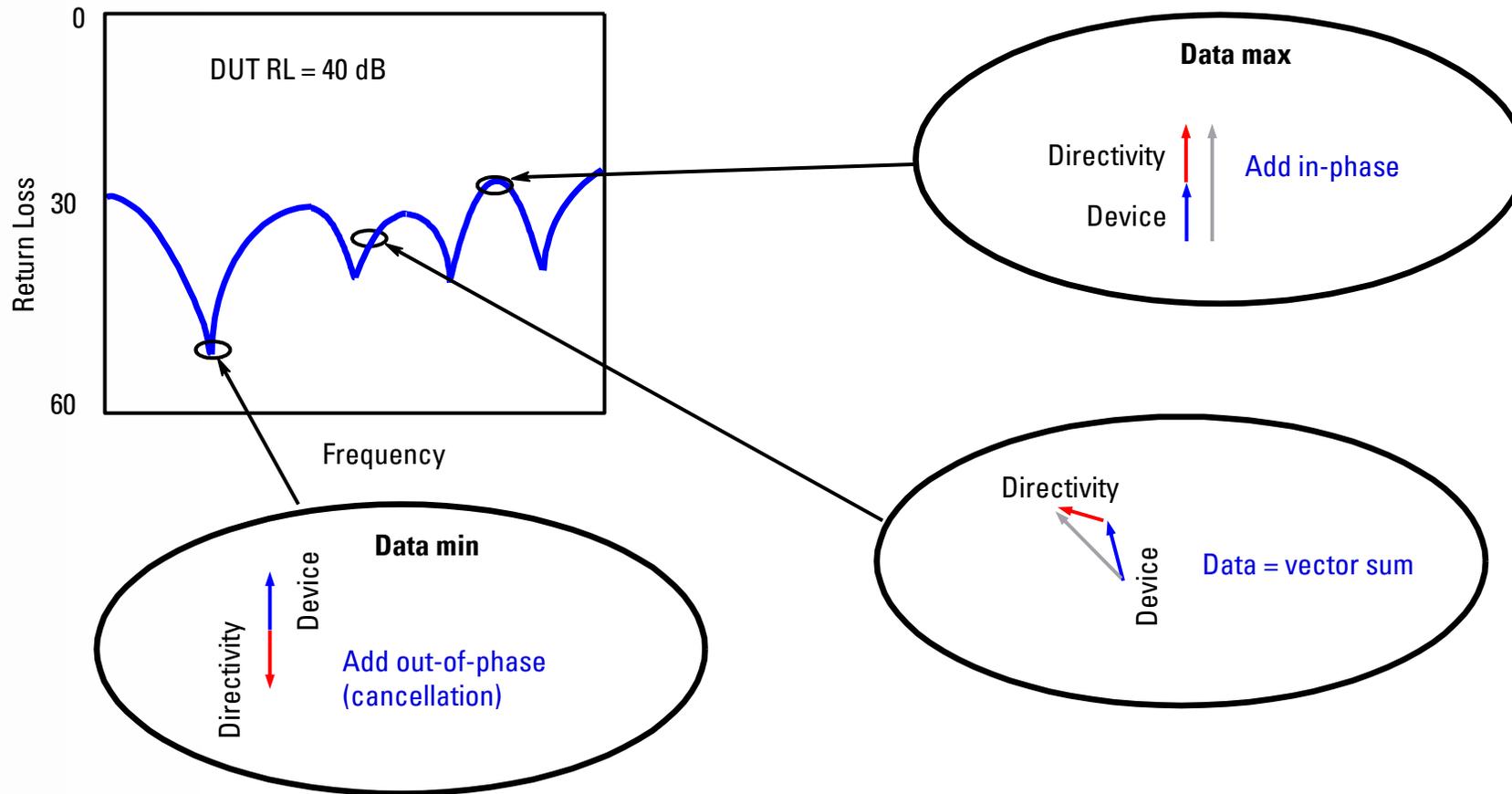
- **Directivity** is a measure of how well a directional coupler or bridge can separate signals moving in opposite directions



$$\text{Directivity} = \text{Isolation (I)} - \text{Fwd Coupling (C)} - \text{Main Arm Loss (L)}$$

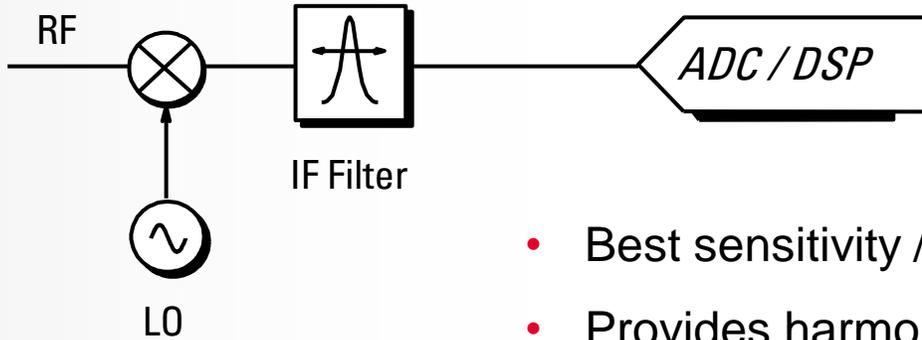
# Interaction of Directivity with the DUT

(WITHOUT ERROR CORRECTION)

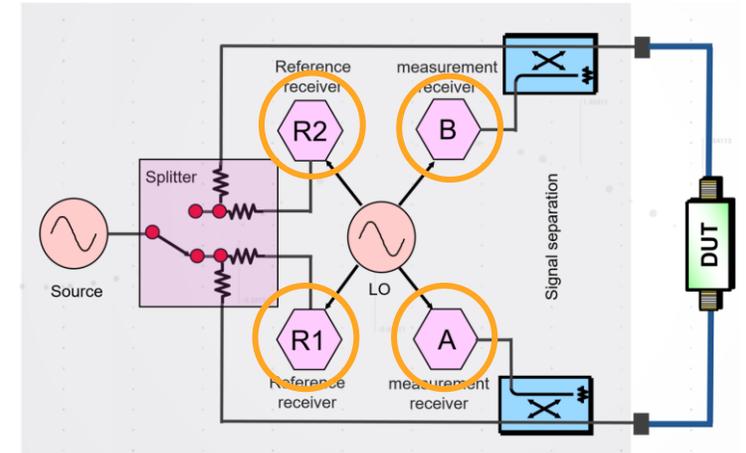
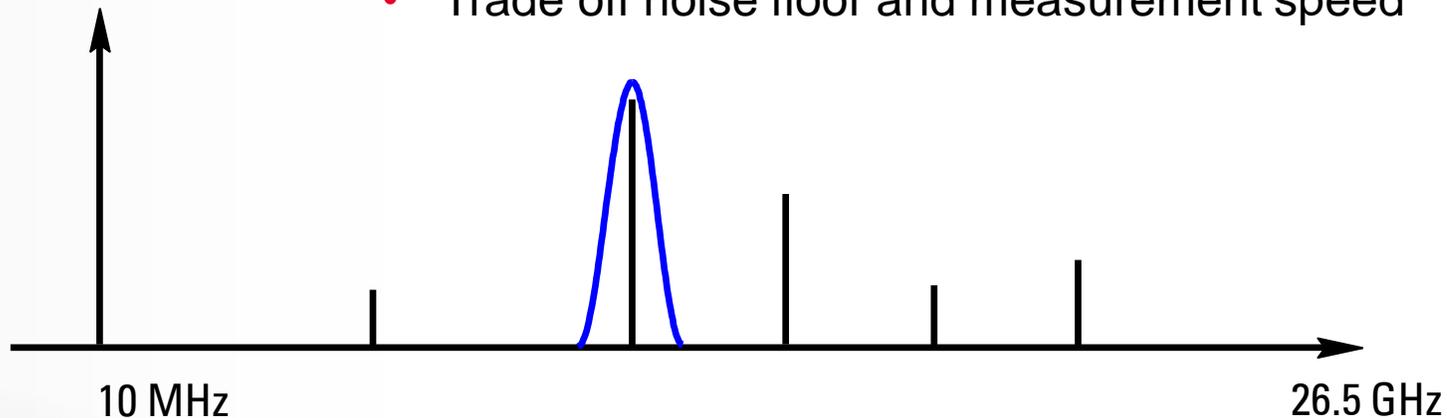


# Receivers

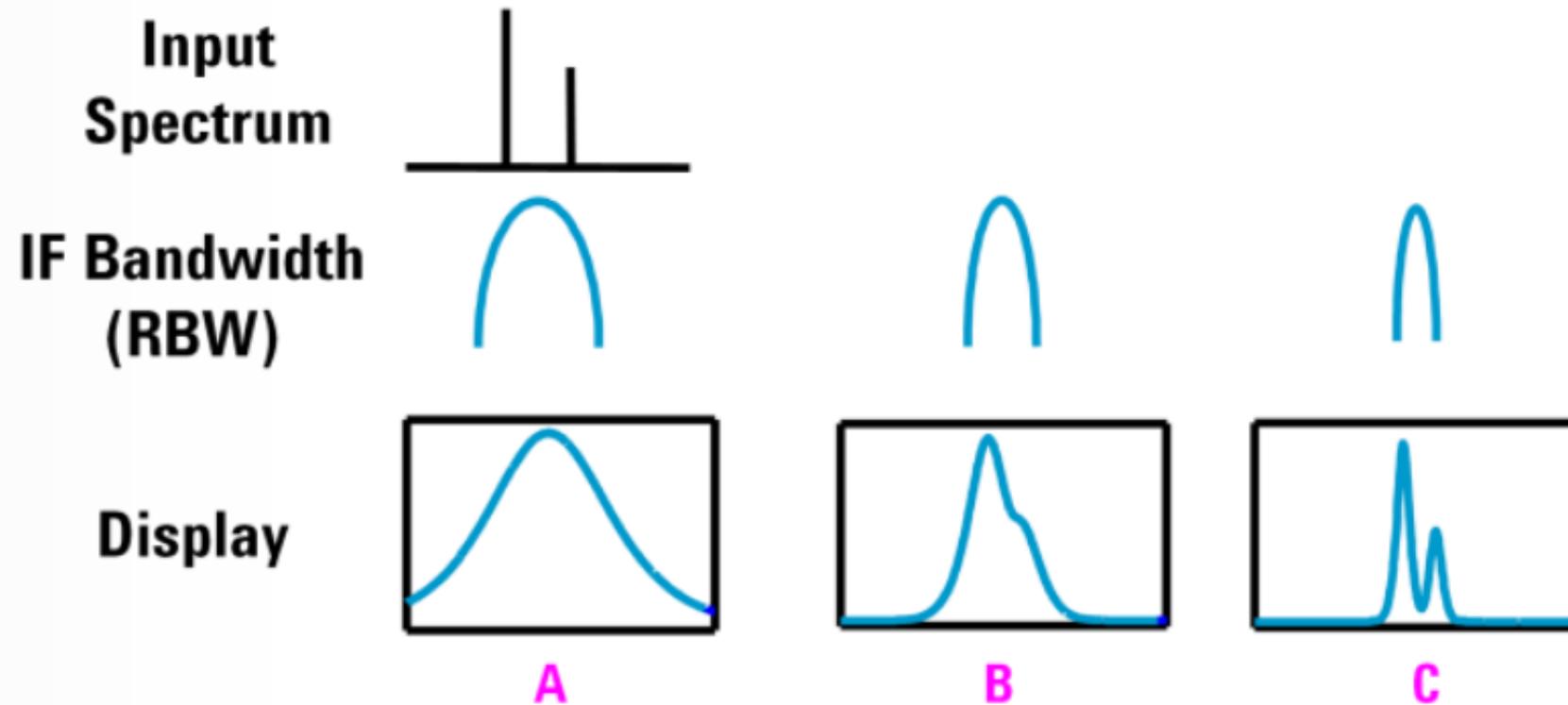
## NARROWBAND DETECTION - TUNED RECEIVER



- Best sensitivity / dynamic range
- Provides harmonic / spurious signal rejection
- Improve dynamic range by increasing power, decreasing IF bandwidth, or averaging
- Trade off noise floor and measurement speed

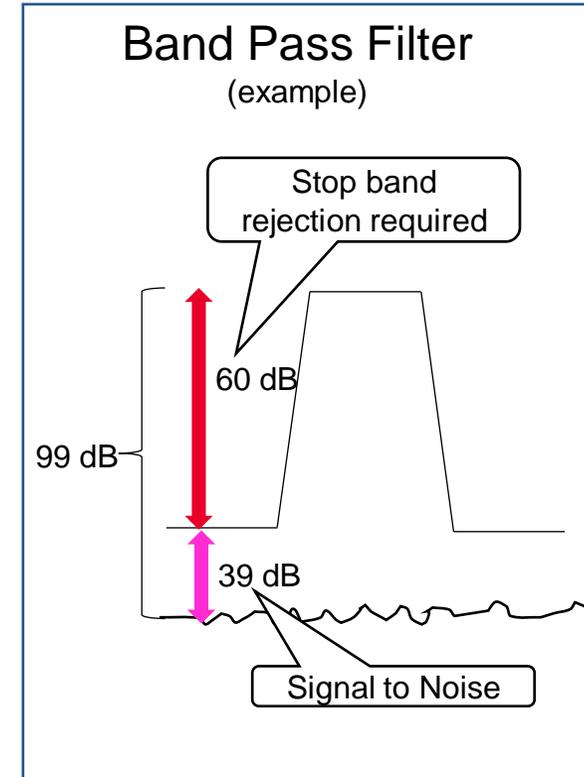
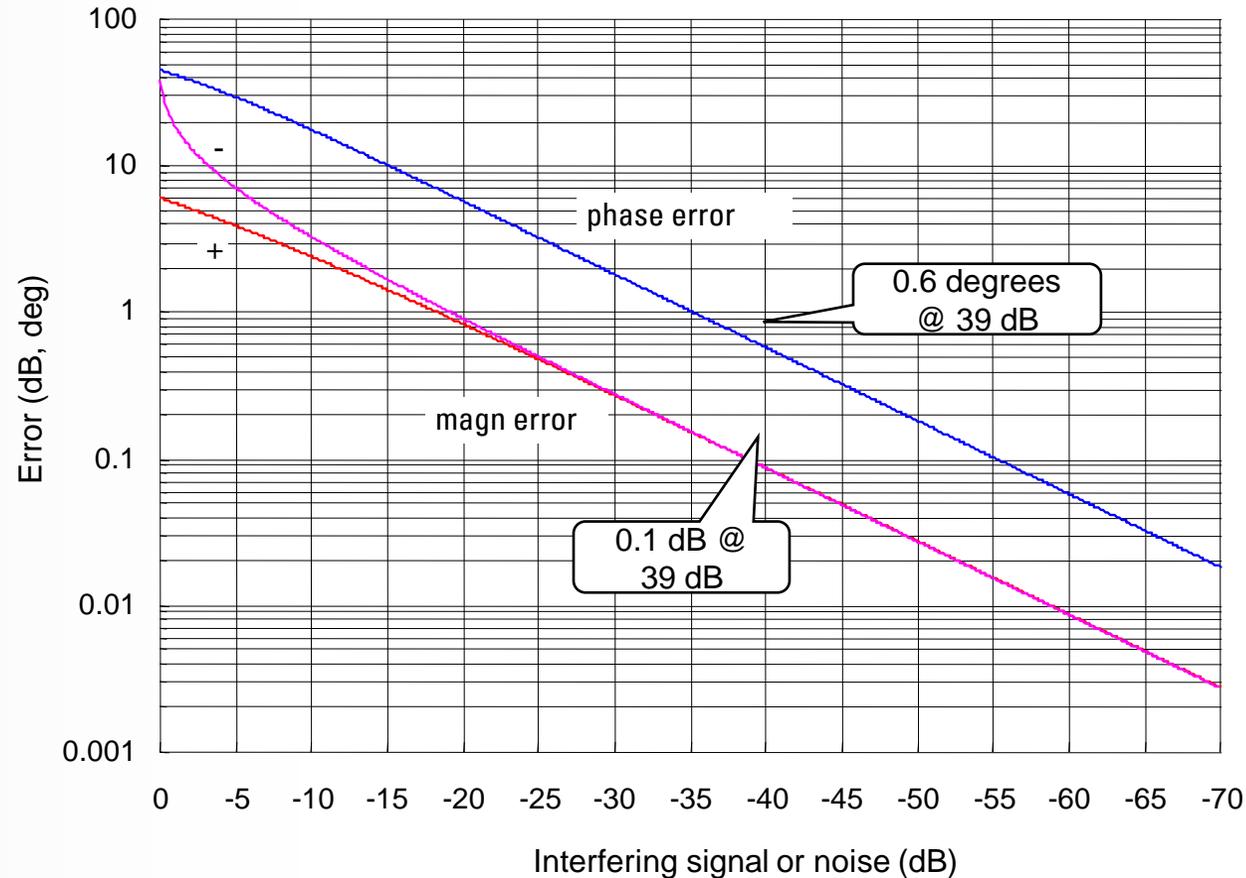


# IF Bandwidth



# Dynamic Range and Accuracy

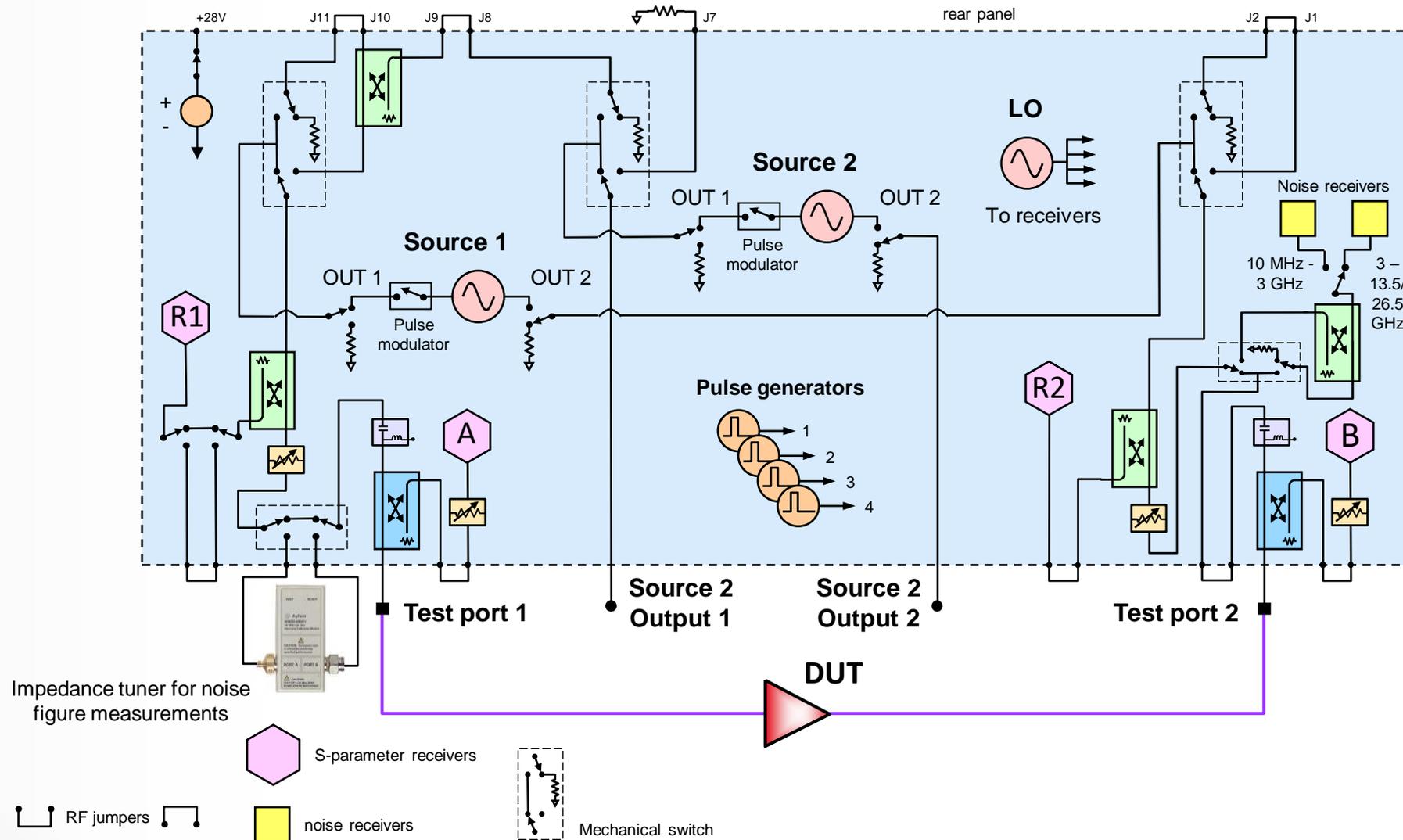
## ERROR DUE TO INTERFERING SIGNAL



Dynamic range for 0.1 dB accuracy = 60 dB (rejection) + 39 dB (SNR) = 99 dB

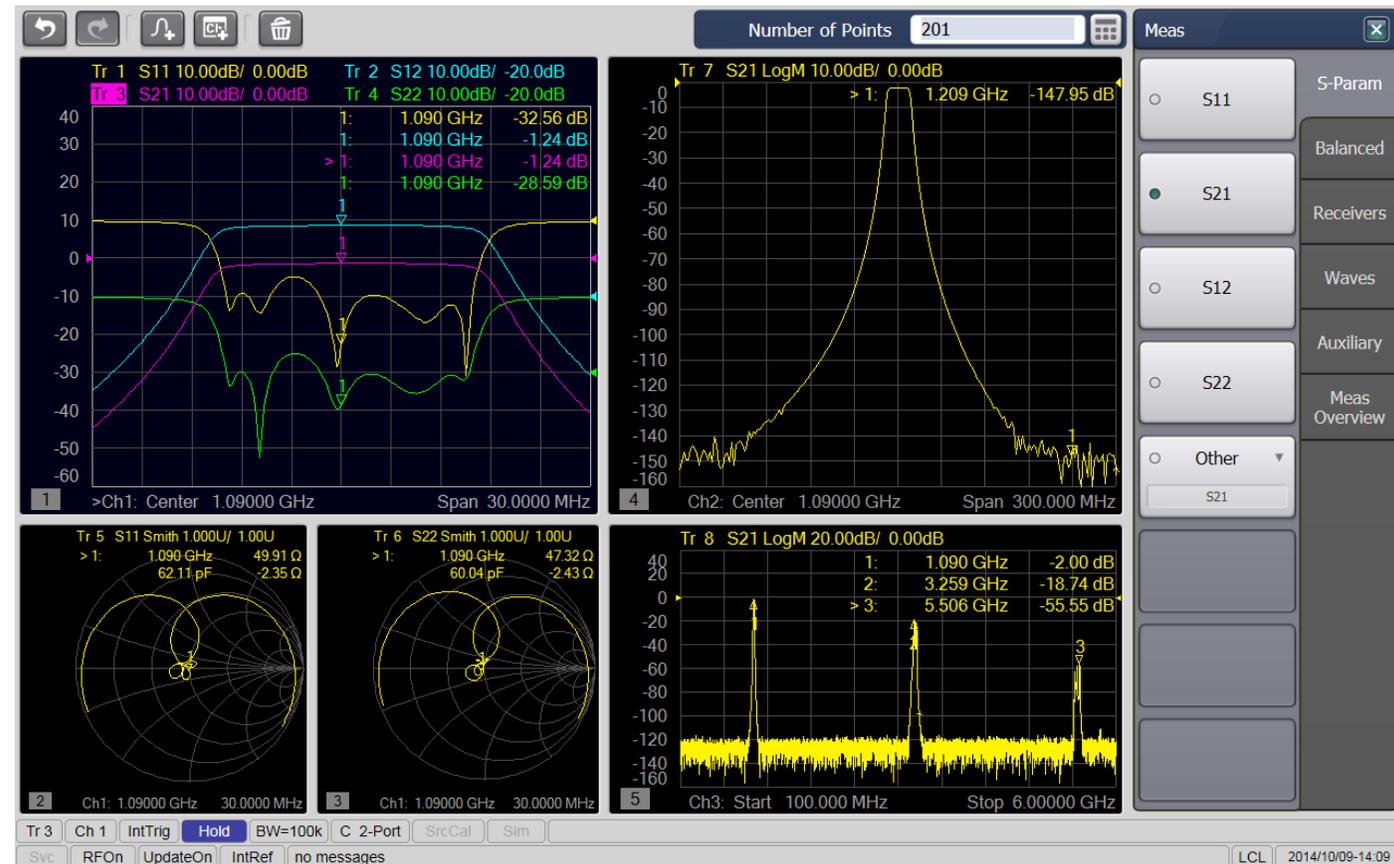
*Dynamic range is very important for measurement accuracy!*

# Modern VNA Block Diagram (2-Port PNA-X)



# Processor / Display

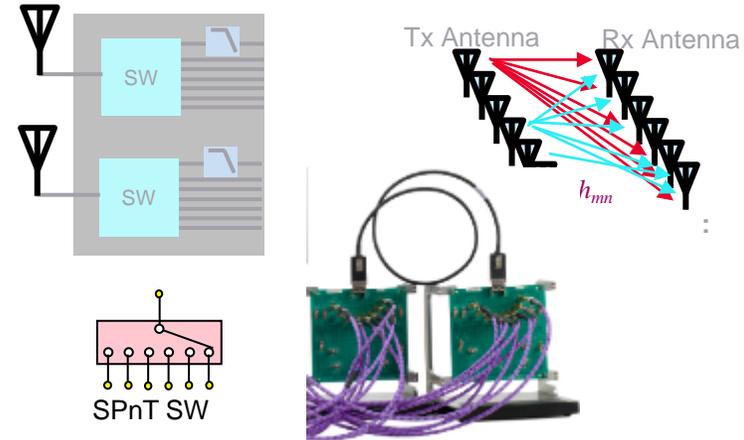
- Markers
- Limit lines
- Pass/fail indicators
- Linear/log formats
- Grid/polar/Smith charts
- Time-domain transform
- Trace math



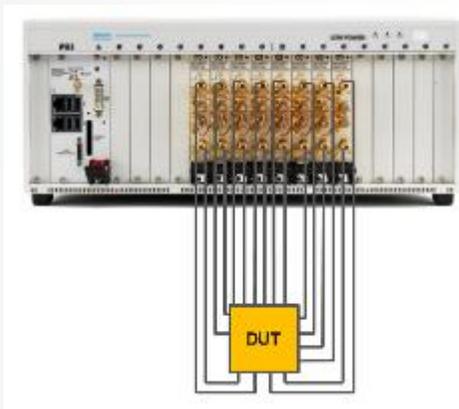
# Multiport Measurement Architectures

## Application Examples

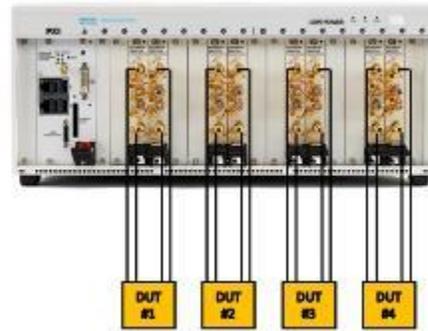
- RF front end modules / antenna switch modules
- Channel measurements of MIMO antennas
- Interconnects (ex. cables, connectors)
- General-purpose multiport devices



## PXI Multiport VNA



## PXI Multi-site VNA



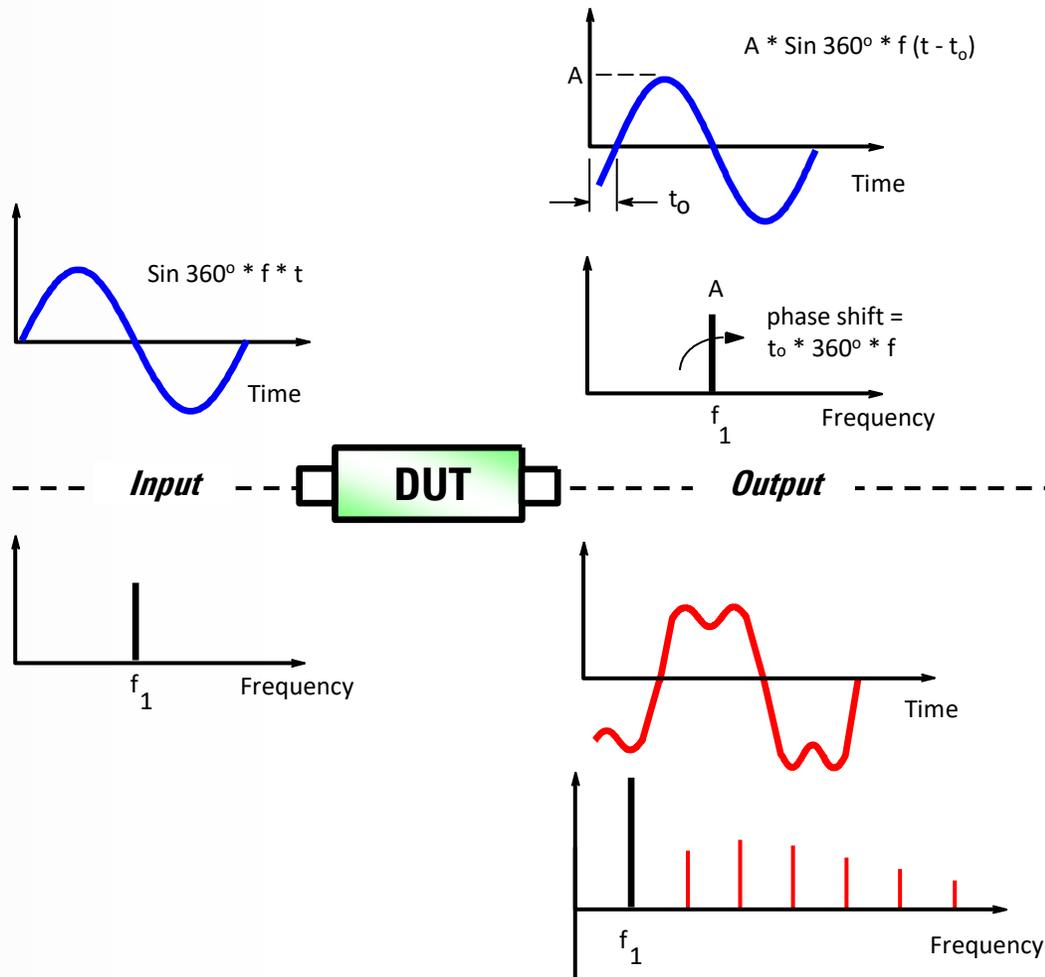
## Key Features

- True multiport VNA with independent modules
- Improved throughput
- High performance without external switches
- Full N-port correction
- Reconfigurable to multiport or multisite

# Agenda

- What is a Network Analyzer?
- Transmission Lines and S-Parameters
- Network Analyzer Block Diagram
- **Network Analysis Measurements**
- Calibration and Error Correction

# Linear Versus Nonlinear Behavior



## Linear behavior:

- Input and output frequencies are the same (no additional frequencies created)
- Output frequency only undergoes magnitude and phase change

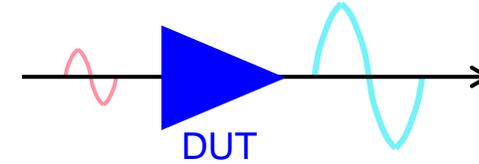
## Nonlinear behavior:

- Output frequency may undergo frequency shift (e.g. with mixers)
- Additional frequencies created (harmonics, intermodulation)

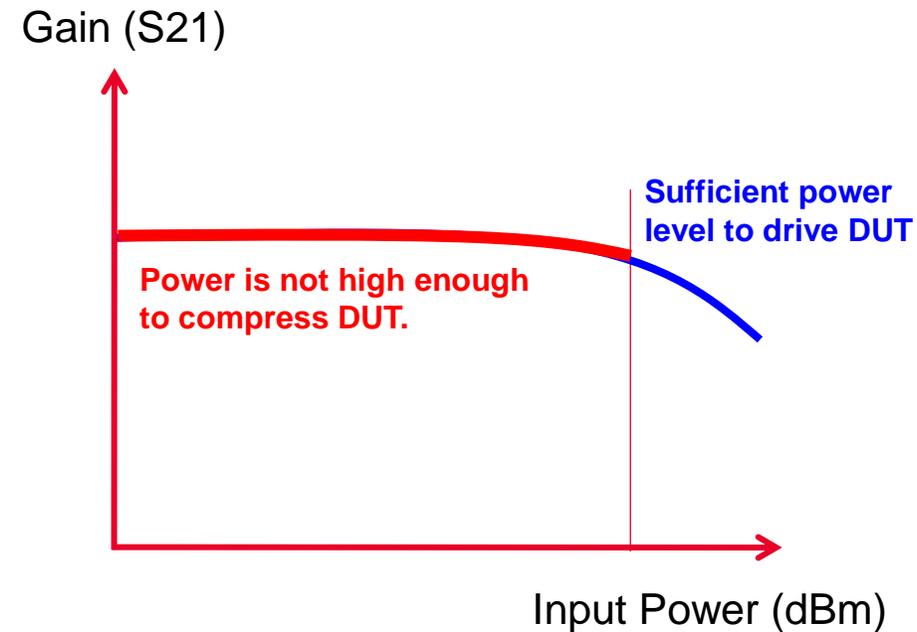
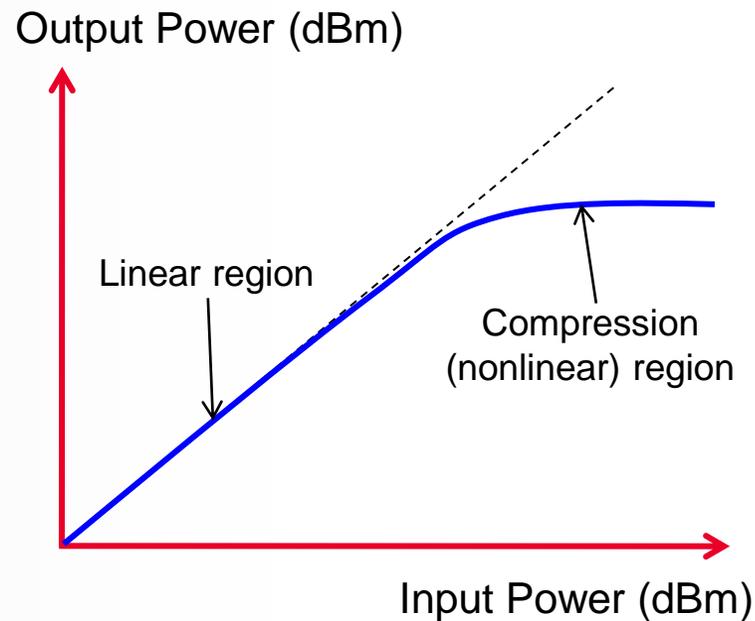
For more information on linear vs. non-linear basics:

<http://literature.cdn.keysight.com/litweb/pdf/5965-7917E.pdf>

# Gain Compression



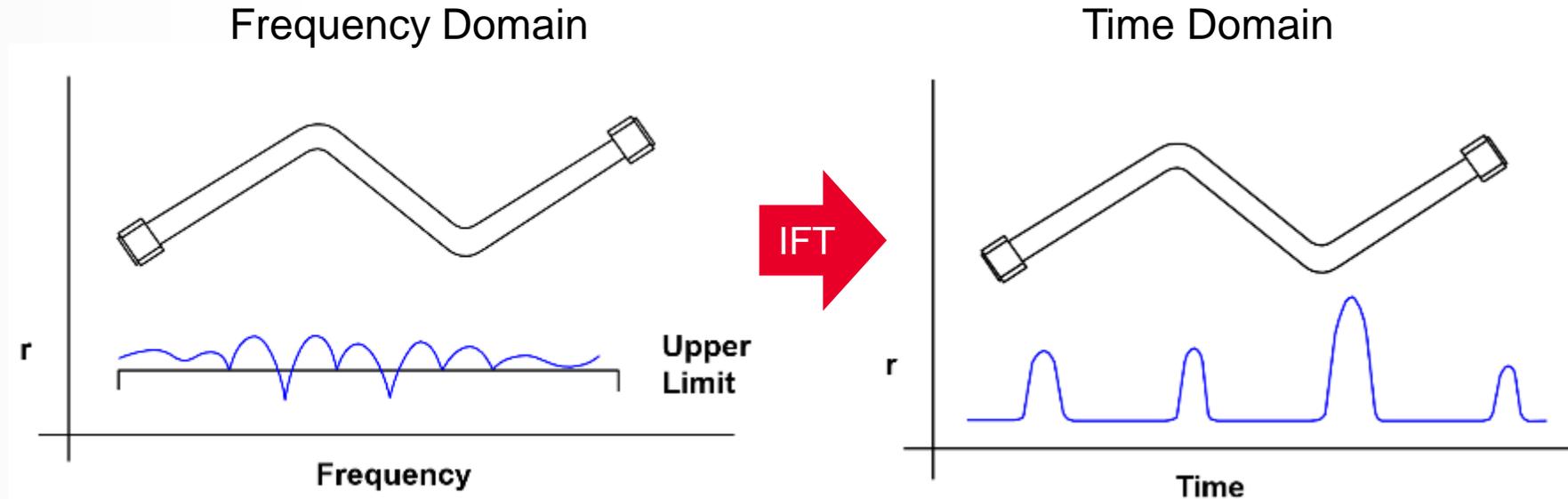
- Parameter to define the transition between the linear and nonlinear region of an active device.
- The compression point is observed as x dB drop in the gain with VNA's power sweep.



Enough margin of source power capability is needed for analyzers.

# Time vs. Frequency Domain

## S<sub>11</sub> RESPONSE OF SEMIRIGID COAX CABLE



- Why time domain?
  - Locate faults
  - Identify passive or inductive circuit elements
  - Identify and remove unwanted fixture responses
  - And more...

For more information on time domain basics:  
<http://literature.cdn.keysight.com/litweb/pdf/5989-5723EN.pdf?id=923465>

# Agenda

- What is a Network Analyzer?
- Transmission Lines and S-Parameters
- Network Analyzer Block Diagram
- Network Analysis Measurements
- Calibration and Error Correction

# The Need For Calibration

- **Why do we have to calibrate?**

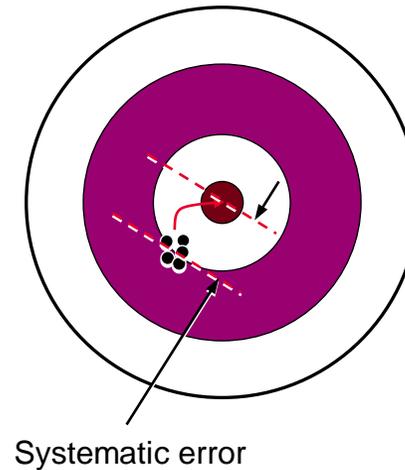
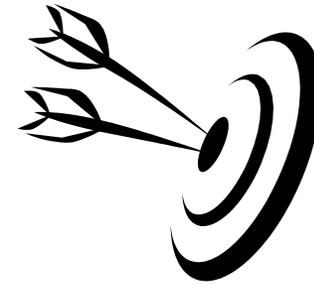
- It is impossible to make perfect hardware
- It would be extremely difficult and expensive to make hardware good enough to entirely eliminate the need for error correction

- **How do we get accuracy?**

- With vector-error-corrected calibration
- Not the same as the yearly instrument calibration

- **What does calibration do for us?**

- Removes the largest contributor to measurement uncertainty: systematic errors
- Provides best picture of true performance of DUT



# Measurement Error Modeling

- **Systematic Errors**



- Due to imperfections in the analyzer and test setup
- Assumed to be time invariant (predictable)
- Generally, are largest sources of error

- **Random Errors**

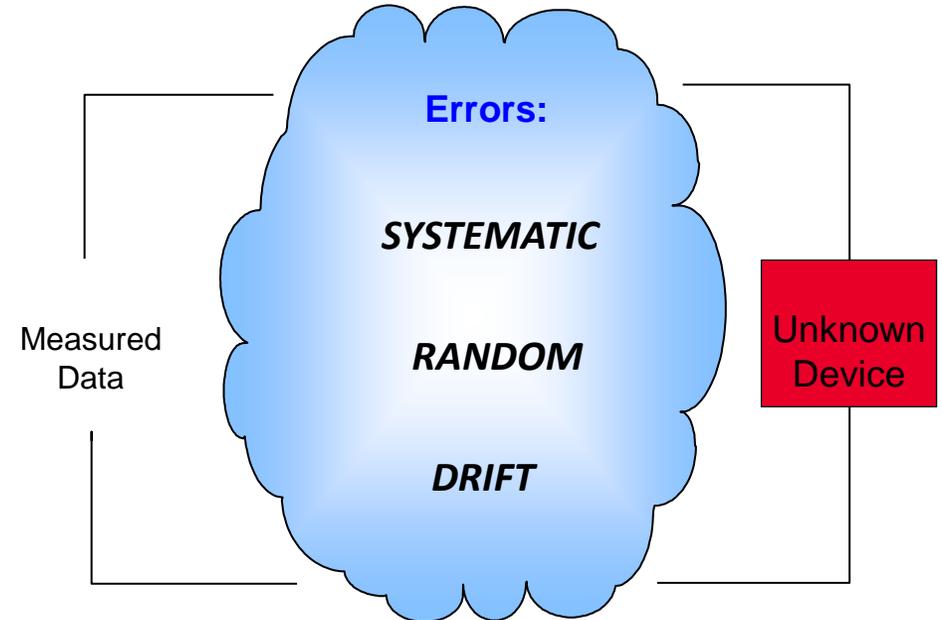


- Vary with time in random fashion (unpredictable)
- Main contributors: instrument noise, switch and connector repeatability

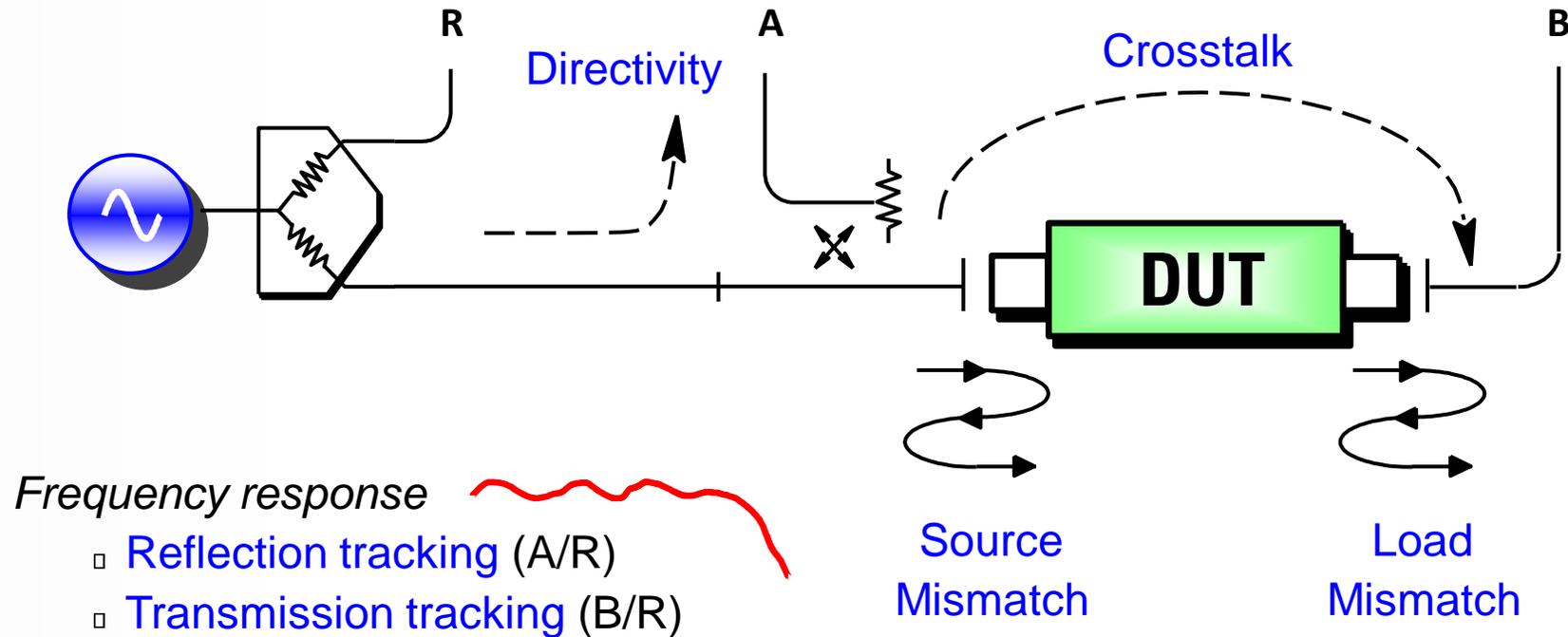
- **Drift Errors**



- Due to system performance changing **after** a calibration has been done
- Primarily caused by **temperature variation**



# Systematic Measurement Errors



**Six forward and six reverse error terms yields 12 error terms for two-port devices**

# Types of Error Correction

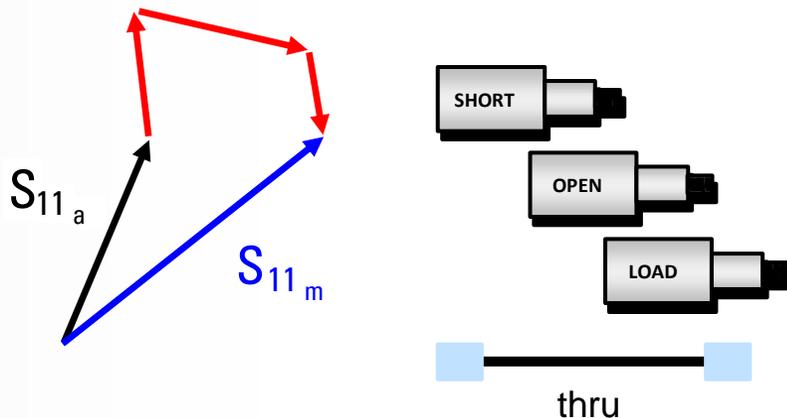
- **Response (normalization)**

- Simple to perform
- Only corrects for tracking (frequency response) errors
- Stores reference trace in memory, then does data divided by memory



- **Vector**

- Requires more calibration standards
- Requires an analyzer that can measure phase
- Accounts for all major sources of systematic error



## Available Standards



Mechanical short, open, load, thru (SOLT)



Electronically switched arbitrary known impedances

# Significance of Calibration

## TYPES OF CALIBRATION

### UNCORRECTED



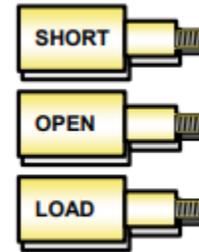
- Convenient
- Generally not accurate
- No errors removed

### RESPONSE



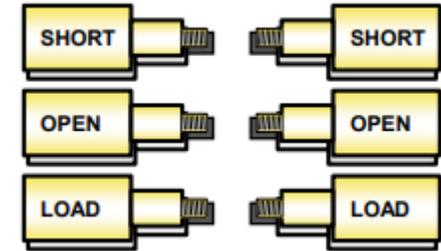
- Easy to perform
- Use when highest accuracy is not required
- Removes frequency response error

### 1-PORT



- For reflection measurements
- Need good termination for high accuracy with 2-port devices
- Removes these errors:
  - Directivity
  - Source match
  - Reflection tracking

### FULL 2-PORT



Defined Thru or Unknown Thru



- Highest accuracy
- Removes these errors:
  - Directivity
  - Source/load match
  - Reflection tracking
  - Transmission tracking
  - Crosstalk (limited by noise)

### ENHANCED RESPONSE

- Combines response and 1-port
- Corrects source match for transmission measurements

# Using Known Standards to Correct for Systematic Errors

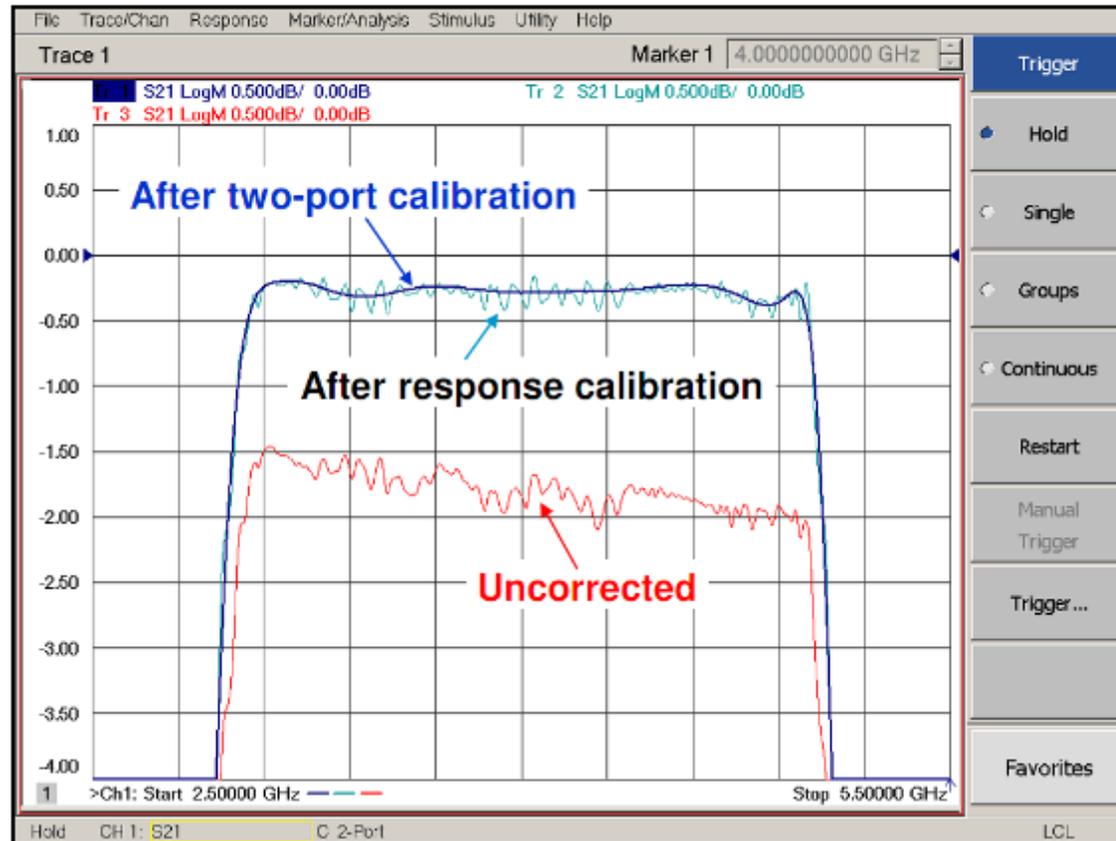
- **Response calibration (normalization)**
  - Only one systematic error term measured
  - Reflection tracking
- **1-port calibration (*reflection measurements*)**
  - Only three systematic error terms measured
  - Directivity, source match, and reflection tracking
- **Full two-port calibration (*reflection and transmission measurements*)**
  - Twelve systematic error terms measured
  - 10 measurements on four known standards (SOLT)
  - 7 measurements using Unknown Thru; 4 measurements using QSOLT
- **Standards defined in cal kit definition file**
  - Network analyzer contains standard cal kit definitions
  - **CAL KIT DEFINITION MUST MATCH ACTUAL CAL KIT USED!**
  - User-built standards must be characterized and entered into user cal-kit

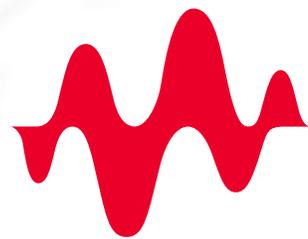


# VNA showing Band Pass Filter

UNCALIBRATED, RESPONSE CAL AND FULL 2 PORT CAL

## Measuring filter insertion loss





**KEYSIGHT**  
**TECHNOLOGIES**